CPU and/or GPU: Revisiting the GPU Vs. CPU Myth

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Abstract

Parallel computing using accelerators has gained widespread research attention in the past few years. In particular, using GPUs for general purpose computing has brought forth several success stories with respect to time taken, cost, power, and other metrics. However, accelerator based computing has significantly relegated the role of CPUs in computation. As CPUs evolve and also offer matching computational resources, it is important to also include CPUs in the computation. We call this the hybrid computing model. Indeed, most computer systems of the present age offer a degree of heterogeneity and therefore such a model is quite natural.

We reevaluate the claim of a recent paper by Lee et al. (ISCA 2010). We argue that the right question arising out of Lee et al. (ISCA 2010) should be how to use a CPU+GPU platform efficiently, instead of whether one should use a CPU or a GPU exclusively. To this end, we experiment with a set of 13 diverse workloads ranging from databases, image processing, sparse matrix kernels, and graphs. We experiment with two different hybrid platforms: one consisting of a 6-core Intel i7-980X CPU and an NVidia Tesla T10 GPU, and another consisting of an Intel E7400 dual core CPU with an NVidia GT520 GPU. On both these platforms, we show that hybrid solutions offer good advantage over CPU or GPU alone solutions. On both these platforms, we also show that our solutions are 90% resource efficient on average.

Our work therefore suggests that hybrid computing can offer tremendous advantages at not only research-scale platforms but also the more realistic scale systems with significant performance gains and resource efficiency to the large scale user community.

1 Introduction

Parallel computing using accelerator based platforms has gained widespread research attention in recent years. Accelerator based general purpose computing, however, relegated the role of CPUs to second-class citizens where a CPU sends data and program to an accelerator and gets the results of the computation from the accelerator. As CPUs evolve and narrow the performance gap with accelerators on several challenge problems, it is imperative that parity is restored by also bringing CPUs in the computation process.

Hybrid computing seeks to simultaneously use all the computational resources on a given tightly coupled platform. We envisage a multicore CPU plus accelerators such as GPUs, see also Figure 1 as one such realization. The CPU in Figure 1 on the left with six cores is connected to a many-core GPU on the right. In our work, we use two variants of the model shown in Figure 1 by choosing different CPUs and GPUs.

The case for hybrid computing on such a platform can be made naturally. Computers come with a CPU, at least a dual-core at present, and is expected to contain tens of cores in the near future. Graphics processing units are traditionally used to process graphics operations and most computers come equipped with a graphics card that presently has several GFLOPS of computing power. Moreover, commodity production of GPUs has significantly lowered their prices. Hence, an application using both a multicore CPU and an accelerator such as a GPU can benefit from faster processing speed, better power and resource utilization,
Figure 1: A tightly coupled hybrid platform.

Figure 2: A view of hybrid multicore computing. Figure (a) shows the conventional accelerator based computing where the CPU typically stays idle. Figure (b) shows the hybrid computing model with computation overlapping between the CPU and the GPU.

and the like. Figure 2 illustrates the benefits of such a hybrid computing model. As can be noticed in Figure 2(b), hybrid computing calls for complete utilization of the available computing resources.

Further, it is believed that GPUs are not well suited for computations that offer little SIMD parallelism, and have highly irregular memory access patterns. For various reasons, CPUs do not suffer greatly on such computations. Thus, hybrid computing opens the possibility of novel solution designs that take the heterogeneity into account. Hence, we posit that hybrid computing has the scope to bring the benefits of high performance computing to also desktop and commodity users.

We distinguish between our model of hybrid computing with other existing models as follows. We consider computational resources that are tightly coupled. Supercomputers such as the Tianhe-1A that use a combination of CPUs and GPUs do not fall in our category. The issues at that scale would overlap with some of the issues that arise in hybrid computing, but have other unique issues such as interconnection network and its cross-section bandwidth, latency, and the like.

Hybrid computing solutions on platforms using a combination of CPUs and GPUs are being studied for various problem classes such as dense linear algebra kernels [5, 45], maximum flows in networks [23], list ranking [48] and the like. Most of these works however have a few limitations. In some cases, for example [23, 48, 44], computation is done only either on the CPU or the GPU at any given time. Such a scenario keeps one of the computing resource idle and hence is in general wasteful in resources. Secondly, we explore a diverse set of workloads so as to highlight the advantages and limitations of hybrid multicore computing. In a departure from most earlier works, we study hybrid computing also on low end CPU and GPU models and see the viability of hybrid computing on such platforms.

The aim of this work is to explore the applicability of hybrid multicore computing to a class of applications. To this end, we select a collection of 13 different workloads ranging from databases to graphs, and image analysis, and present hybrid algorithmic solutions for these workloads. Some of the results that we show in this paper are reported recently [8, 9, 18, 15, 33], or under submission [10]. We identify two different algorithm engineering approaches that we have used across our 13 workloads. Further, these approaches can be used to classify most of the recent works on hybrid computing including [45, 20]. The two approaches are described briefly in the following:

- **Work Sharing**: In a work sharing approach where the problem is decomposed into one or more parts, with each part running on a different machine in the hybrid computing platform. In this approach, the
work shares have to be chosen appropriately so as to balance the load on the CPU and the GPU. In this approach, the actual algorithm used on the different units could be different, and in some cases, may also be different from the best possible algorithm on each device respectively. For example, see our hybrid algorithm for graph connected components and sparse matrix-vector multiplication described in Section [4].

- **Task Parallel:** A task parallel approach involves viewing the computation as a collection of interdependent tasks, and tasks are mapped on to the available units. In this setting, one has to think of arriving at the best possible mapping that minimizes the overall span and also minimizes the idle time of machines. As can be seen, the time taken by a hybrid solution using task parallelism is the time corresponding to the longest path in the task graph with nodes and edges labelled by the time taken to complete the task and communication time respectively.

A slight modification to the task parallelism approach is that of pipelined parallelism. A pipelined parallelism approach views the computation as a clever combination of the units to set up a pipeline that has different functionalities at each stage of the pipeline.

1.1 Our Contributions

Some of the specific contributions of our study are as follows.

- We develop new hybrid solutions for seven of the 13 workloads studied in this paper: sorting, histogram, spmv, bilateral filtering, convolution, ray casting, and the Lattice Boltzman Method.

- We experiment with a hybrid system consisting of a six core Intel i7 980X (Westmere) CPU and an NVidia Tesla T10 GPU. On this hybrid platform, called Hybrid-High, we show that hybrid computing has an average of 29% performance improvement over the best possible GPU-alone implementation. Our solutions also exhibit 90% resource efficiency on average.

- To promote the idea that hybrid computing has benefits on more widely used platforms, we also experiment with a hybrid platform that has an Intel Core 2 Duo E7400 (Allendale) with an NVidia GT520 GPU. We feel that such configurations still have the potential to make supercomputing affordable and accessible to everyone. On such a platform, called Hybrid-Low, we show that hybrid computing results in an average of 37% performance improvement compared to the best possible GPU-alone implementation. Our solutions also exhibit 90% resource efficiency on average.

- We analyze the above results and offer insights on the limits and applicability of hybrid computing in the present architectural space.

The title of our paper is motivated by a recent related paper [46] that argued about the relative strengths of GPUs and multicore CPUs on a set of throughput oriented workloads. We establish through this paper that accelerator based computing should leverage the combined strengths of all devices in a computing platform via hybrid computing. A majority of our workload overlap with the workloads considered in [46].

1.2 Organization of the Paper

The rest of the paper is organized as follows. Section 2 discusses the architectures of the GPUs and the CPUs used in our paper. Section 3 describes the workloads that we study in this paper. Section 4 outlines some of the important implementation perspectives of our hybrid algorithms. Section 5 discusses the outcomes of our hybrid solutions and analyzes the solutions. The work is put in the right context by discussing related prior work in Section 6. The paper ends with concluding remarks in Section 7.
2 Hybrid Computing Platforms

In this section, we briefly describe the two hybrid CPU+GPU computing platforms that we use in our study.

2.1 The Hybrid-High Platform

One of the hybrid computing platform we use in this paper, labeled Hybrid-High, is a combination of a six core Intel i7 980X CPU with an NVidia Tesla T10 GPU. The Intel i7 980X CPU that we use in our experiments is a six core machine with each core running at 3.4 GHz and with a thermal design power of 130 W. The six physical cores are hyper-threaded so that together they can run 12 threads. Other features of the i7 980X include a 32 KB instruction + 32 KB data L1 cache per core, a 256 KB L2 cache per core, and a large shared 12 MB L3 cache shared by all 6 cores. The memory bandwidth is up to 1066 MHz.

The GPU is a massively multi-threaded processor containing hundreds of processing elements or cores, called the Scalar Processors (SPs). The Tesla C1060 is add-on card based on the Tesla T10 GPU[36] having SPs arranged in groups of eight. It has 30 such SMs, which makes for a total of 240 processing cores. Each of the cores are clocked at 1.3 Ghz. These eight SP execute in a Single Instruction Multiple Thread (SIMT) fashion. Hence, all the SPs in an SM execute the same instruction at the same time.

The CUDA API allows a user to create a large number of threads to execute code on the GPU. Threads are also hierarchically grouped into blocks and grids. Blocks are serially assigned for execution on each SM. Each of the blocks are made of several warps which execute in each core in a SIMD fashion. For more details, we refer the interested reader to [35].

2.2 The Hybrid-Low Platform

We also experiment with a hybrid platform, called Hybrid-Low, that resembles a desktop computing environment more closely. The Hybrid-Low platform is a combination of an Intel Core 2 Duo E7400 CPU along with an NVidia GT520 GPU.

The Intel Core 2 Duo CPU is one of the earliest multicore offerings from Intel and was released in the year 2008. It has 2 cores with hyper-threading and each of the cores are clocked at 2.8 GHz. The CPU consists of a 3 MB L2 cache and the maximum power consumption is around 65 W. The CPU was designed entirely for commodity PCs which gives a sustained performance of about 20 GFLOPS.

The GT520 is a stand-alone graphics processor having 48 computing cores and 1 GB of global memory. Each of the compute cores are clocked at 810 MHz. The GPU on an average give a sustained performance of 77.7 GFLOPS and consume about 29W of power. In this system both the processors are of a comparable performance range and hence provide a more realistic platform for experimenting the hybrid programs.

3 Workloads

In this paper, we experiment with the following workloads. Table 3 summarizes the characteristics of the various workloads considered.

**Sorting:** Sorting is one of the fundamental operations in information processing that has many applications. Recent results on efficient implementations of sorting are reported in [34, 3], to name a few. This workload becomes an important case study due to the large number of applications. For the purposes of this paper, we focus on comparison-based sorting techniques and leave non-comparison based sorting technique such as radix sort out of the scope.

**Histogram:** One of the important operations in image processing is to compute the histogram of the intensity values of the pixels. Computing the histogram of a dataset in parallel typically requires the use of atomic operations. The nature of this workload such as use of atomic operations and being memory bound make this a good case study for hybrid computing.
<table>
<thead>
<tr>
<th>Workload (Short name)</th>
<th>Application Area</th>
<th>Nature</th>
<th>Characteristics</th>
<th>Solution Methodology</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sorting sort</td>
<td>Semi-numerical, databases</td>
<td>regular</td>
<td>compute bound</td>
<td>work sharing+ task parallel</td>
</tr>
<tr>
<td>Histogram hist</td>
<td>image processing</td>
<td>Atomics,</td>
<td>memory bound irregular</td>
<td>work sharing</td>
</tr>
<tr>
<td>Sparse matrix-vector</td>
<td>Sparse Linear Algebra</td>
<td>irregular</td>
<td>memory bound</td>
<td>work sharing</td>
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<tr>
<td>multiplication spmv</td>
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<tr>
<td>Sparse matrix-matrix</td>
<td>Sparse Linear Algebra</td>
<td>irregular</td>
<td>device storage, memory bound</td>
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<tr>
<td>Ray casting RC</td>
<td>Image processing</td>
<td>irregular</td>
<td>compute bound</td>
<td>work sharing</td>
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<td>Bilateral filtering Bilat</td>
<td>Image processing</td>
<td>regular</td>
<td>compute bound</td>
<td>work sharing + task parallel</td>
</tr>
<tr>
<td>Convolution Conv</td>
<td>Image processing</td>
<td>regular</td>
<td>compute bound</td>
<td>work sharing</td>
</tr>
<tr>
<td>Monte-carlo MC</td>
<td>Physics, computational finance</td>
<td>regular, pseudorandom numbers</td>
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<tr>
<td>List Ranking LR</td>
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<td>Connected Components CC</td>
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<tr>
<td>Lattice Boltzeman Method LBM</td>
<td>Computational Fluid Dynamics</td>
<td>irregular</td>
<td>memory bound</td>
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<tr>
<td>Image Dither Dither</td>
<td>Image processing</td>
<td>irregular</td>
<td>causal dependencies</td>
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<tr>
<td>Bundle adjustment Bundle</td>
<td>Image processing</td>
<td>irregular</td>
<td>memory bound</td>
<td>task parallel</td>
</tr>
</tbody>
</table>

Table 1: Various workloads considered in this paper.
Sparse Matrix-Vector Multiplication (spmv): Efficient operations involving sparse matrices are essential to achieve high performance across numerical applications such as climate modeling, molecular dynamics, and the like. In most of the above applications, spmv computation is the main bottleneck. Hence, efforts to speed up this computation on modern architectures have attracted significant research attention in recent years [49, 16]. Further, the computation involved in spmv is highly irregular in nature due to the sparsity of the matrix.

Sparse matrix-matrix multiplication (spgemm): Another operation that is important with respect to sparse matrices is that of multiplying two sparse matrices. This workload has found applications spanning several areas such as graph algorithms [26], numerical analysis including computation fluid dynamics [37, 21, 16] and is also included as one of the seven dwarfs in parallel computing in the Berkeley report [4]. Some of the recent works that have reported efficient sparse matrix multiplication on modern architectures are [13]. It is generally accepted that the difficulties of this workload include its irregular nature of computation, the difficulty in predicting the size of the output and the concomitant memory management problems.

Both spmv and spgemm are important linear algebra kernels with significant applications, and hence their choice is justified.

Ray casting: This is a fundamental problem in image analysis and computer graphics. Recent applications to medical image analysis are also reported [42]. As all rays perform the computations independently, the problem is very much portable for parallel architectures. Tracing multiple rays in an SIMD fashion is challenging, because rays access non-contiguous memory locations, resulting in incoherent and irregular memory accesses. The choice of this workload is justified because of the range of applications of ray casting to visual computing.

Bilateral filter: Bilateral filter is an edge-preserving and noise reducing filter used in image processing. It is a non-linear filter in which intensity value at any pixel is equal to a weighted sum of intensities in the neighbourhood. The filter involves transcendental operations like computing exponentials, which can be very computationally expensive. Hence, it is a compute bound problem with regular memory access.

Convolution: Convolution is a common operation used in image processing for effects such as blur, emboss and sharpen. Given the image signal and the filter, the output at each pixel is equal to the weighted sum of its neighbours. Since each pixel can be computed independently by a thread, there is ample parallelism available. The computations increase with the size of filter and exhibits high compute to memory ratio.

The bilateral filtering and convolution workloads are commonly used filters in image processing applications, justifying their inclusion on our workloads.

Monte-carlo: Monte Carlo methods are used in several areas of science to simulate complex processes, to validate simpler processes, and to evaluate data. In Monte Carlo (MC) methods, a stochastic model is constructed in which the expected value of a certain random variable is equal to the physical quantity to be determined. The expected value of this random variable is then determined by the average of many independent samples representing the random variable. This workload exhibits a regular memory access pattern and is compute bound, typically. The choice of this workload is justified by the wide body of applications using Monte Carlo methods across varied domains such as computational finance, physics, and engineering.

List Ranking: The importance of list ranking to parallel computing has been identified by Wyllie as early as 1978 in his Ph. D. thesis [50]. The list ranking problem is to find the distance of every node from one end of the given linked list. The workload is memory bound due to the highly irregular nature of the computation involved. The workload is chosen as a case study as list ranking is often a primitive in several graph and tree based computations.

Connected Components: Finding the connected components of a given undirected graph has been a fundamental graph problem with several applications. Ideas used in parallel algorithms for connected components find immediate application to other important graph algorithms such as minimum spanning trees and the like. Hence, this workload is important and offers good scope as a case study.

Lattice Boltzman Method: Lattice Boltzman Method (LBM) refers to a class of applications from
computational fluid dynamics (CFD) and are used in fluid simulations. It is a numerical method that solves the Navier–Stokes equation via the discrete Boltzman equation. In this work, we study the D3Q19 lattice model where over a three dimensional cubic lattice, each cell computes the new function values based on its 19 neighbors [22]. The LBM operation is highly data parallel. This workload is considered for its applications to computational fluid dynamics.

**Image Dithering:** In Floyd-Steinberg Dithering (FSD) (see [18]), we approximate a higher color resolution image using a limited color palette by diffusing the errors of threshold operation to the neighboring pixels according to a weighted matrix. The problem is thus inherently sequential and poses enormous challenge for a parallel implementation, let alone a hybrid implementation. Dithering has various applications such as printing, display on low-end LCD or mobile devices, visual cryptography, image compression, and the like. Further this workload is significant because of its atypical nature amongst image processing applications that does not offer embarrassing parallelism.

**Bundle Adjustment:** It refers to the optimal adjustment of bundles of rays that leave 3D feature points onto each camera center with respect to both camera positions and point coordinates. Bundle Adjustment is carried out using the Levenberg-Marquardt (LM) algorithm [32, 38] because of its effective damping strategy to converge quickly from a wide range of initial guesses. Bundle adjustment often is the slowest and the most computationally resource intensive step. It is one of the primary bottlenecks in the Structure-from-Motion pipeline, consuming about half of the total computation time.

4 Implementation Details

In this section, we describe the implementation details of the various workloads described in Section 3. For the workloads including sort, Bilat, Conv, spmv, hist, RC, and LBM we developed hybrid implementations for the purposes of this paper. In some cases, we use implementation developed in recent existing works that are known to be the best possible. Workloads LR, CC, Dither, MC, spgemm, and MC fall under this category. For more details on these implementations, we refer the reader to the technical reports available at [28].

4.1 Sorting

Our implementation of sorting is a comparison based sorting algorithm based on the techniques of sample sort reported in [34]. Sample sort involves placing the elements into various bins according to a number of splitters. For sorting, we apply the basic principle of work partitioning in a hierarchical fashion. We, first compute the histogram of the data in a hybrid manner. Using the histogram results we perform the binning process. As, the histogram provides a good estimate of the distribution of the data, the binning process consumes a much lesser overhead. However, on the initial iteration of the kernel, the individual bins that are created are large in size and cannot be directly used for sorting. In order to optimally sort each of the bins, we reduce the size of each of the bins down to a certain threshold where groups of 32 elements can be compared by a single warp. Each of these warps will in effect implement quick sort on the 32 elements. We recursively run the binning process to reduce the bin sizes to the chosen threshold. The CPU on the other hand, will not be limited by the compute as much as the GPU. We can hence still leave the bin sizes of the CPU at a higher threshold than that of the GPU. We also notice that there is a clear trade-off in the number of recursive calls to split the elements into bins, and the time taken to sort the bins independently.

4.2 Histogram

The histogram operation in a parallel setting requires the proper use of atomic increment operations to ensure consistent and reliable results. We use the work sharing approach where we divide the data set into two sets for the GPU and the CPU. We then perform the computation of the histogram on both the devices in an overlapped fashion. This step is followed by a simple addition of the results from the two devices. On the
GPU, using shared memory is critical in order to reduce the global memory latency. The atomic increment is performed by a single warp working on the data that is obtained from the shared memory. The histogram in general is a bandwidth bound problem and hence, proper use of the memory channels are essential. The shared local cache (L1) in the CPU is used to improve the performance. The resulting partial histograms are then added bin-by-bin to give the final histogram result over the entire input data.

4.3 spmv

In the spmv workload, some of the challenges faced by modern architectures include the overhead of the auxiliary data structures, irregular memory access patterns due to the sparsity of the matrix, load balancing, and the like. Several recent works [11] have therefore focussed on optimizing the spmv computation on most modern architectures.

In our hybrid implementation, we use a novel work sharing based solution summarized as follows. In spmv, we notice that the computation involving one row is independent of the computation involving other rows. This suggests that one should attempt a work sharing based solution. Instead of splitting the computation according to some threshold, we use the following novel work sharing approach. Our approach is guided by the fact that typically spmv is used over multiple iterations. So, one can rely on preprocessing techniques that aim to improve the performance of spmv.

Notice that the GPUs are good at exploiting massive data parallelism with regular memory access patterns. Therefore, we assign the computation corresponding to the dense rows to the GPU and the computation corresponding to the sparse rows to the CPU. The exact definition of sparsity is estimated via experimentation. In this direction, we first sort the rows of the matrix according to the number of nonzeros. We then rearrange the matrix according to increasing order of the number of nonzeros. We also rearrange the x vector and then assign the computation corresponding to the dense rows to the GPU and the sparse rows to the CPU. The entire x vector is kept at both the CPU and the GPU. This therefore suggests that when using the work sharing approach, one can divide the computation according to what computation is more suitable for each of the architectures in the hybrid platform.

On the CPU, we use the Intel MKL [1] library routines and on the GPU we use the CUSP library routines. These are known to be offer the best possible results on each platform.

4.4 spgemm

For the spgemm workload, one can see that computations on various rows of the input matrices are independent of each other. So, we use a work sharing model in our hybrid implementation. We use the Intel MKL library [1] for computations on the CPU, and use a row-row method based implementation developed by us recently in [33] for the GPU computations. The main implementation difficulty experienced in this workload is to arrive at the appropriate work shares. The work share would be dictated primarily by the volume of the output. Since estimating the volume of output is as hard as actually multiplying the matrices, one has to rely on heuristics to arrive at the work share. In our implementation, we use the runtime of a CPU alone implementation and a GPU alone implementation to obtain the work share.

On the CPU, we use the Intel MKL [1] library routines and on the GPU we use the Row-Row method of matrix multiplication. The row-row method works as follows [33]. In $C_{m \times n} = A_{m \times p} \cdot B_{p \times n}$, the $i$th row $C$, denoted $C(i,:)$, is computed as $\sum_{j \in A(i,:)} A(i,j) \cdot B(j,:)$. This formulation works best on GPUs for sparse matrices as only those elements that contribute to the output are accessed. For more details of the Row-Row method on the GPU, we refer the reader to [33].

4.5 Ray Casting

In ray casting, rays can perform the computations independently. Therefore, the problem is very much portable for parallel architectures. Tracing multiple rays in an SIMD fashion is however challenging because

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rays access non-contiguous memory locations, resulting in incoherent and irregular memory access.

We notice that there are two main steps in ray casting. The first step is to find the first triangle that is intersected by each ray. This is then used to find the first tetrahedron intersected. The second step involves tracing the ray from the first hit point and traversing the ray through the entire mesh to keep accumulating the intensity values from the interpolation function. The computation for this step finishes once the ray leaves the mesh.

In our hybrid implementation, we used a work sharing based solution model since the computation for each ray can be performed independently. However, the nature and amount of computation in the above two steps differs significantly. For this reason, we proceed as follows. We ensure that computation for each ray finishes the first step before starting computation for the second step for any ray. The work share across the two steps is also varied to reflect the varied nature of the computation across the two steps. The work share for each step is obtained empirically by studying the time taken by the CPU and the GPU individually on each of the two steps. We notice that the optimal work shares across the two steps vary significantly depending on the platform.

### 4.6 Bilateral Transforms and Convolution

The workload of bilateral filtering poses interesting challenges. The workload has regular memory access patterns, offers good work sharing, and is compute bound. Bilateral filtering has the following mathematical equation on an input image $I$ and $O$ being the output image.

In our hybrid implementation, we use a combination of task parallelism and work sharing approach. Notice that bilateral filtering involves computing transcendental functions that are very time consuming on the GPU. The number of unique such function evaluations are however limited by the filter size in case of the spatial filter, and by the number of different intensity values in the case of the range filter. The largest filter size of interest is typically $15 \times 15$. So, there are only 225 different values that have to be evaluated for the spatial filter. Given that the intensity values for the images under consideration were between 0 to 255, the range filter also has only 255 unique values to the computed. We perform these computations on the the multicore CPU and transfer the results to the GPU. This use of novel task parallelism in our hybrid implementation proved to be quite beneficial and serves to illustrate the advantages of a hybrid computing platform.

Given the values of the transcendental functions in the form of look-up tables, applying the filter can be done on parts of the image independently. So, we use the work sharing approach and divide the input image $I$ into two parts: $I_{CPU}$ and $I_{GPU}$. The CPU and the GPU computations apply the filter on the above image parts respectively. The size of the partitions is arrived at empirically.

On both the CPU and the GPU, our implementation proceeds by each thread reading a set of pixels and applying the filter using the look-up tables. Additionally on the GPU, we make use of shared memory by having each thread block load the required image from the global memory to the shared memory.

For the convolution workload, we observe that the computation is very regular, compute bound, and is also highly amenable to data parallel operations. As is the standard approach in most GPU implementations and other modern architectures, we imagine that each thread is computing on a small portion of the image. To take advantage of the hybrid computing platform, we divide the computation into two parts according to a certain threshold. The multicore CPU computes the convolution of a part of the image $I_{CPU}$ and the GPU computes on the rest of the image, say $I_{GPU}$. The threshold is chosen as follows. It is observed, (cf. [46]), that the GPU has about a 3x time advantage compared to multicore CPUs. As the exact model of the CPU and the GPU used in the study of [46] is comparable to that of our platform, we start with the assumption that the threshold could be around 25%. We then fine tune the actual threshold by experimentation. On the CPU, we utilize the availability of the Intel MKL implementation that is known to be by far the most efficient implementation of convolution on multicore CPUs. For the GPUs, we use our own custom implementation. For more details, we refer the reader to [30].
4.7 Monte Carlo

Monte Carlo applications typically involve several iterations each using pseudorandom numbers to estimate the expected value of a random variable of interest. We chose the application of photon migration from [12]. In the hybrid solution, we use a hybrid pseudorandom number generator that we developed in [8]. In photon migration, several photons are launched with their position and direction initialized to either zeros (for some pencil beam initialized at the origin) or some random numbers. At every step a photon takes, a fraction of its weight is absorbed, and then photon packet is scattered. The new direction and weight of photon are updated. After several such steps if the remaining weight of a photon is below a certain threshold, the photon is terminated.

4.8 List Ranking and Connected Components

For the list ranking workload, we summarize the approach used in [9, 8]. We start by preprocessing the linked list to reduce the size of the list from \( n \) nodes to a size of \( n/\log n \) using ideas from fractional independent sets. We then use the algorithm of Hellman and Jaja [24] to rank the list of remaining elements. Finally, the ranking is extended to the elements removed from the list during the preprocessing phase. For the preprocessing, we require that each node in the linked list choose a bit among \( \{0, 1\} \) independently and uniformly at random. For this, we use the multicore CPU to generate a stream of pseudorandom numbers. These numbers are then transferred to the GPU so that each node can access the pseudorandom numbers when it requires.

In the CC workload, as reported in [9], we notice that the best possible algorithms for sequential processing, such as DFS, and PRAM-style parallel algorithms use fundamentally different techniques. Therefore, we use the following approach that divides the computation across the multicore CPU and the GPU. The input graph \( G \) is partitioned into two induced subgraphs, \( G_1 = G[V_1] \) and \( G_2 = G[V_2] \) where \( V(G) = V_1 \cup V_2 \) and \( V_1 \cap V_2 = \Phi \). We use BFS on the CPU cores to find the connected components in the graph \( G_1 \) and the algorithm of Shiloach and Vishkin [41] on the GPU to find the connected components in the graph \( G_2 \). In the above computation, edges with exactly one end point in either \( V_1 \) or \( V_2 \) are not included. We call such edges as cross edges. Hence, in a final step, the connected components of \( G_1 \) and \( G_2 \) are combined using the cross edges. This final step is done on the GPU. The size of \( V_1 \), and hence the size of \( V_2 \), is fixed using an experimentally obtained threshold.

4.9 LBM

The LBM workload is highly parallelizable since each particle can be distributed to each thread of computation. The Lattice Boltzman model simulates the propagation and collision processes of a large number of particles. We perform the simulation over cubic lattices. A standard notation in LBM is the \( DnQm \) scheme. The parameter \( n \) stands for the dimensions of the cubic lattice, and \( m \) stands for the number of “speeds” studied. In this work, we study the D3Q19 lattice model where over a 3-dimensional cubic lattice, each particle computes the new function values based on its present values.

The computations of various functions are independent of each other. So, in our hybrid implementation, we use a task parallel solution approach. Given the relative speeds of the CPU and the GPU, we choose to compute four functions on the CPU and the remaining 15 functions are computed on the GPU. Each GPU thread is assigned the computation with respect to one particle. This can be seen to improve the data coalescing effects on GPU.

4.10 Image Dithering and Bundle Adjustment

For the image dithering workload, we use different strategies to perform FSD on the CPU and the GPU. On multi-core CPUs, we formulated a block based approach as this reduces the total threads required, which is favorable to the multi-core CPUs. For many-core GPUs, we operate at the pixel level since many-core
GPU architecture is suited for larger number of light weight threads. We notice that as we use both the CPU and the GPU in a work sharing model, we need to transfer at most three floating point numbers from the CPU to the GPU. We therefore were able to arrive at an efficient hybrid solution. More details of this implementation appear in [18].

For the bundle adjustment workload, we decompose the LM algorithm into multiple steps, each of which is performed using a kernel on the GPU or a function on the CPU. Our implementation efficiently schedules the steps on CPU and GPU to minimize the overall computation time. The concerted work of the CPU and the GPU is critical to the overall performance gain. The implementation that we use here appears in [15].

5 Results and Discussion

In this section, we start by describing our evaluation methodology, the results obtained, and then discuss the results in the context of hybrid computing.

<table>
<thead>
<tr>
<th>Workload</th>
<th>Dataset</th>
<th>Hybrid-High Gain%</th>
<th>Hybrid-Low Gain%</th>
<th>Hybrid High Idle Time%</th>
<th>Hybrid Low Idle Time%</th>
</tr>
</thead>
<tbody>
<tr>
<td>sort</td>
<td>uar</td>
<td>18.6</td>
<td>28.9</td>
<td>13.3</td>
<td>9.1</td>
</tr>
<tr>
<td>hist</td>
<td>uar</td>
<td>32.3</td>
<td>21.8</td>
<td>47.7</td>
<td>27.9</td>
</tr>
<tr>
<td>spmv</td>
<td>[49]</td>
<td>15.1</td>
<td>48.4</td>
<td>1.2</td>
<td>1.1</td>
</tr>
<tr>
<td>spgemm</td>
<td>[49]</td>
<td>38.9</td>
<td>41.87</td>
<td>1.76</td>
<td>0.41</td>
</tr>
<tr>
<td>RC</td>
<td>[39, 31]</td>
<td>23.8</td>
<td>39.7</td>
<td>10.3</td>
<td>8.9</td>
</tr>
<tr>
<td>LBM</td>
<td>uar</td>
<td>15.0</td>
<td>11.6</td>
<td>27.4</td>
<td>23.5</td>
</tr>
<tr>
<td>Bilat</td>
<td>uar</td>
<td>12.9</td>
<td>7.22</td>
<td>1.5</td>
<td>1.5</td>
</tr>
<tr>
<td>Conv</td>
<td>uar</td>
<td>23.5</td>
<td>41.0</td>
<td>0.04</td>
<td>0.04</td>
</tr>
<tr>
<td>MC</td>
<td>uar</td>
<td>15.7</td>
<td>16.8</td>
<td>6.0</td>
<td>4.78</td>
</tr>
<tr>
<td>LR</td>
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<td>33.9</td>
<td>4.2</td>
<td>9.11</td>
</tr>
<tr>
<td>CC</td>
<td>[6]</td>
<td>45.16</td>
<td>56.4</td>
<td>2.85</td>
<td>3.76</td>
</tr>
<tr>
<td>Dither</td>
<td>uar</td>
<td>25.5</td>
<td>10.5</td>
<td>8.9</td>
<td>6.42</td>
</tr>
<tr>
<td>Bundle</td>
<td>[43]</td>
<td>88.4</td>
<td>78.8</td>
<td>77.0</td>
<td>*</td>
</tr>
</tbody>
</table>

Table 2: Summary of results of our implementations on the Hybrid-High and the Hybrid-Low platforms. The phrase "uar" in the second row refers to the dataset that contains items drawn uniformly at random appropriate for the workload. A citation in the second row indicates that we have used the datasets from the work cited. The performance gain indicated is according to the following metric: time for sort and hist, GFLOPS for spmv, time for spgemm, frames per second for RC, time for LBM, M pixels/Sec for Bilat and Conv, and time for MC, LR, CC, Dither, and Bundle. For the Bundle workload, the idle time on Hybrid-Low platform is not available.

5.1 Evaluation Methodology

On the platforms described in Section 2 we have used OpenMP specification 3.0 [2] and CUDA 4.0 [35] to implement our hybrid solutions. Our GPU programs also use standard optimization techniques such as coalesced memory access, use of shared memory, minimizing thread divergence, and the like. The hybrid programs are optimized according to best practices for hybrid solutions such as minimizing the overall execution time, minimizing the idle time for any device, asynchronous transfer of intermediate values between the devices, and the like.

We are interested in two aspects of hybrid solutions. Firstly, we want to study the benefits of hybrid computing. We define the gain of a hybrid solution as the ratio of the time taken by the hybrid program to
the minimum time required by a pure GPU or a pure CPU solution. Secondly, by nature, hybrid solutions should minimize the amount of time any of the device is idle. We define the idle time of a hybrid solution as the total time any device in the hybrid platform is not used in the computation. This could be due to waiting for results from other device, or not allotted any part of the computation, or not allotted enough part of the computation. A low idle time indicates better resource efficiency.

5.2 Results

Table 2 summarizes the results of our hybrid solutions. The second row of Table 2 specifies the dataset used in our study. The entries in the third and the fourth row are the percentage improvement of hybrid solutions using the Hybrid-High and the Hybrid-Low platforms respectively. The fifth and the sixth row of the Table shows the idle time of our hybrid solutions on both the platforms considered. The performance gain and the idle times are for the largest input sizes for all workload except spmv, spgemm. For these two workloads we use the average measurement over all the instances in the dataset considered [19]. The values reported in Table 2 and Figure 3[a]–[l] are the average over multiple runs. The results of Table 2 indicate that our hybrid solutions offer an average of 30% improvement on the Hybrid-High platform, and an average of 34% on the Hybrid-Low platform. Remarkably, the Hybrid-Low platform whose configuration is likely to match commonly used desktop configurations also offers good incentives for hybrid computing.

Figure 3[a]–[l] show the performance of our hybrid implementations on various inputs from the datasets mentioned in the second row of Table 2. The plots in Figure 3 show that our hybrid implementations scale well over increasing input sizes. In most cases, our maximum input size is limited only by the available memory on the GPU in the hybrid platform.

On most workloads, our results on the Hybrid-High and Hybrid-Low platforms suggest that hybrid computing has scope and advantage. Our workloads also have applications in common settings such as graphics and image manipulation, data processing, and the like. Some of these operations are invoked internally by regular users of computers such as gamers. The input sizes that we used in evaluating the Hybrid-Low platform are also close to the typical usage in most cases.

5.3 Analysis of the Results

In this section, we analyse the results shown in Section 5 in the context of our evaluation methodology.

5.3.1 Performance of Hybrid Solutions

Some of our workloads such as Conv, Bilat are very amenable to the GPU style of computation. On such workloads, as can be noticed from Table 2, the hybrid advantage on the Hybrid-High platform is rather modest. This is accentuated by the fact that the GPU in the Hybrid-High platform has a peak throughput that is 10 times that of the CPU in the Hybrid-High platform when considering single precision operations. On the Hybrid-Low platform however, as the ratio of the peak throughput of the GPU and the CPU is smaller, hybrid computing can be seen to offer a decent advantage even on regular workloads.

On the other hand, about half our workloads have irregular memory access patterns that are known to be very difficult for GPUs to handle. Examples of such workloads include LR, spgemm, CC, and the like. On such workloads, as can be observed from Table 2 hybrid computing on the Hybrid-High platform offers better than 40% advantage on workloads such as LR even while the GPU peak throughput is about ten times that of the peak CPU throughput. This is possible by using novel task mapping techniques that assign the right task to the right processor. This suggests that as GPUs suffer on workloads with highly irregular memory access patterns, one should think of utilizing the power of hybrid computing.

For the workloads that are common to the workloads considered in [46], our GPU alone results are either better or comparable than those reported in [46]. Since the CPU used in [46] is different from the CPUs we used in our hybrid computing platforms, it is not possible to compare the CPU alone performance.
Figure 3: The plots show the performance improvement (in percentage) of hybrid solutions over a pure GPU solution for the workloads considered over various input sizes.
5.3.2 Idle Time

Table 2 also shows the idle time of our workloads on both the platforms. For workloads that use a work sharing parallel approach, it can be observed that the idle time is quite small. This is due to the fact that at the right threshold of work distribution, the CPU and the GPU take near identical times.

For workloads using a task parallel solution approach, such as LBM, and Bundle, it is possible that the computation time is not matched between the CPU and the GPU. In the case of LBM and Bundle, further fine-tuning of the task assignment is also not possible. In the case of Bundle adjustment workload, there is no equivalent Pure-GPU code as the hybrid code is a direct extension of the available CPU code. Some tasks are not amenable to a further sub-division which means that computation on those tasks would always result in an imbalance on the CPU and the GPU runtime. In such cases, the idle time tends to be high.

5.4 Discussion

In this section, we try to highlight some of the lessons that were learnt during our study in hybrid computing. These can offer some insights into how future heterogeneous architectures at the commodity scale and also at the higher end can be designed.

5.4.1 Communication Cost

In most of the hybrid computing solutions, it is required that the devices transfer intermediate results or other such data related to the progress of the computation. For instance, in the sorting workload, in our hybrid implementation, as the GPU further splits bins which have more than a pre-selected number of elements, the CPU is sorting the bins with fewer elements. To enable this, we send the starting and ending indices of the bins with fewer elements that the CPU can sort.

Ideally, one likes to hide this communication with computation. However, at present, computing on CPU-GPU hybrid platforms is difficult as the communication bandwidth between the CPU and the GPU is via the PCI Express link. On the Hybrid-High platform, the peak bandwidth offered is about 6 GB/s. This limitation means that hybrid solutions have to think of novel ways to minimize the amount of communication, hide communication latencies with other computations, and possibly avoid communication. These may also limit the nature of techniques that can be used in hybrid solution design.

In future, therefore, one has to conceive hybrid architectures with a more tighter coupling between the devices so that communication costs can be minimized. Emerging models such as the Intel MIC and the AMD Fusion may offer some hope in this direction and deserve a careful future study.

5.4.2 The Right Solution Methodology

In Section 1, we have identified two broad solution methodologies that hybrid algorithms use, namely task parallelism and work sharing. As we use these two approaches for the 13 workloads presented in this paper, we discuss which approach may be suitable for a given problem.

The work sharing solution methodology involves dividing the work between the CPU and the GPU so that both take roughly the same computation time. This solution methodology is useful when the computation on a part of the input is almost independent of the computation on the other part of the input. For instance, in the Conv workload, the computation on each pixel is dependent only on the values of the neighboring pixels in the input image. This property allows computation on one sub-image to be treated independent of the rest of the image. Similar observations apply to the spmv workload.

The task parallel approach is useful when the computation can be seen as a set of tasks and their dependencies. It may be useful to also represent the tasks and their dependencies as a task graph naturally. Further, the tasks should be such that there exists tasks that are more efficient on a particular architecture. For instance, in the LR workload, we identify tasks such as generating pseudo-random numbers and computing a
fractional independent set (FIS) as two tasks. However, dependent tasks executing on different devices implies that the results of one task have to be necessarily communicated to the other task. The communication time has to be taken into account when mapping the tasks to the devices.

5.4.3 Identifying the Right Threshold in Work Sharing

The work sharing approach to hybrid computing suggests that the CPU and the GPU in the hybrid platform split the overall work in some ratio. This solution methodology is used in workloads such as sort, hist, MC, spgemm, Bilat, and Conv.

In this case, one can see that the work distribution should ideally be according to the ratio of the processing times on the CPU and the GPU in the platform. For instance, if the GPU alone runtime is $T_{GPU}$ and the CPU alone runtime is $T_{CPU}$, then the hybrid solution should split work as $\frac{T_{GPU}}{T_{GPU}+T_{CPU}}$ percentage on the CPU and the remaining percentage on the GPU. The calculation indicates an ideal scenario where all intermediate communication is hidden by useful compute, and no post-processing of the partial results obtained by the CPU and the GPU is required. An example is shown in Figure 4 where the input image is split in a ratio of 18%. One can therefore use the above calculation to identify a good work distribution to start with and then adjust it experimentally after also taking into account the communication times and the post-processing involved.

5.4.4 Identifying and Mapping Work Units in the Task Parallel Approach

Some of our hybrid solutions use the technique of task parallelism. In this technique, we identify work units, or tasks, and their inter-dependence in terms of their precedences. These tasks are then mapped onto the best possible device according to the architectural suitability. We discuss two issues in this context that affect the performance of hybrid solutions.

Firstly, it is not easy in general to identify the right tasks, as computing is often traditionally understood in a sequential step-by-step manner. Even in parallel computing, the intention in general is to speed up each step of the computation using the available processors. Only recently are other methodologies for parallel computing such as using domain specific languages [19, 25] are gaining attention. While these languages alleviate the job of writing efficient parallel programs, they can still be constrained by a traditional step-by-step approach of problem solving.

Identifying the tasks and their dependencies requires a careful reinterpretation of the computation involved. For instance, in the Bilat workload, we noticed that GPUs are not amenable to computing transcendental functions. These were therefore executed on the CPU. Further, it is also noticed that there are really very few transcendental function evaluation that are required for a given image. (These are based on the maximum difference between the pixel intensities). Therefore, we precompute these values, and transfer these values from the CPU to the GPU. While we may be precomputing more values than needed in an actual input, the benefits of this model stem from the fact that recomputing transcendental functions is rather expensive on any architecture.
The LR workload offers similar insights. Our implementation of list ranking in a hybrid setting [9] has a preprocessing phase that requires a large quantity of random numbers. These random numbers can be generated on the CPU and transferred to the GPU. In our implementation, we generate the random numbers on the CPU and the GPU uses the random numbers thus supplied. This is seen to save a lot of processing time in the hybrid setting. Figure 5 shows the task assignment used in our hybrid implementation LR.

Secondly, it is not easy to identify the right task for the right processor. At present, our arguments are based on intuitive reasoning backed by experimental evidence. In future, we would like to study formal mechanisms to arrive at an appropriate and near-optimal task mapping. In fact, arriving at an optimal assignment can be easily seen to be an NP-complete problem and hence one should consider near-optimal assignments.

5.4.5 Lessons for other Hybrid Computing Platforms

Heterogeneity in architectures is a common phenomenon in recent times. Therefore, hybrid computing is poised to play a great role so as to improve resource efficiency. It is hence important to understand how applications can treat the heterogeneity as an advantage. In this section, we extrapolate the lessons learnt from this paper for other hybrid computing platforms and architectural recommendations for the same.

Our experience with the Hybrid-Low platform suggests that the computing devices in a hybrid platform should have similar peak performance capabilities. However, heterogeneity helps by allowing the right task to be executed on the right device. The current trend in equipping architectures with special purpose accelerators such as MMX units, CRC units, encrypt/decrypt units, therefore allows for more task parallel hybrid solutions. Having dedicated accelerators can also make processor design less complex, and also allows for simpler frequency scaling thereby improving power efficiency.

6 Related Work

There has been considerable interest in GPU computing in recent years. Some of the notable works include scan [40], spmv [11], sorting [34], and the like. Other modern architectures that have been studied recently include the IBM Cell and the multi-core machines. Bader et al. [7] have studied list ranking on the Cell architecture and show that by running multiple threads at each SPU, list ranking using the Hellman-JaJa algorithm can be done efficiently. Other notable works on the Cell architecture include [47, 49]. Williams et al. [49] have studied the spmv kernel on various multi-core architectures including those from Intel, Sun, and AMD. Since most of the above cited works do not involve hybrid computing, we do not intend to cite all such works in this paper and refer the reader to other natural sources.

A recent work that motivated this paper is the work of Lee et al. [46]. In [46], Lee et al. argue that GPU computing can offer on average only a 3x performance advantage over a multicore CPU on a range of 14 workloads deemed important for throughput oriented applications. Some of our workloads overlap theirs [46]. Their paper also generated a wide amount of debate on the applicability and limitations of GPU computing. Our view however is that it is not a question of whether GPUs can outperform CPUs or vice-versa, but rather what can be achieved when GPUs and CPUs join forces in a viable hybrid computing platform. Further, for the workloads that are included also in [46], we provided our own GPU and CPU implementations. In workloads such as Bilat, we use novel ideas such as precomputing the transcendental on the GPU for a pure GPU implementation that improve the performance beyond what is reported in [46].
Hybrid computing is gaining popularity across application areas such as dense linear algebra kernels \([5, 45, 20]\), maximum flows \([23]\), graph BFS \([26]\) and the like. The aim of this paper is to however evaluate the promise and the potential of hybrid computing by considering a rich set of diverse workloads. Further, in some of these works, (cf. \([26, 23, 48]\)), while both the CPU and the GPU are used in the computation, one of the devices is idle and while the other is performing computation. In contrast, we seek solutions where both the devices are simultaneously involved in the computation.

There have been recent works that propose benchmark suites for GPU computing. Popular amongst them are the Rodinia \([14]\) and SHOC \([17]\). Some of our workloads such as sorting, \(\text{spgemm}\) are part of the SHOC Level one benchmark suite. Subsets of the workloads considered in our paper appear in other benchmarking efforts related to parallel computing. The Berkeley report \([4]\) lists dwarfs as computational patterns that have wide application. Workloads such as \text{sort, hist, spmv, sgemm}\, are part of Berkeley dwarfs. This serves to illustrate the wide acceptance of our chosen workloads.

### 7 Conclusions

In this paper, we have evaluated the case for hybrid computing by considering workloads from diverse application areas and two different hybrid platforms. We also experimented with two hybrid platforms and analyzed their suitability for hybrid computing. Our study opens the way for evaluation on other challenges with respect to hybrid computing such as power efficiency, benchmark suites, and performance models for hybrid computing (see \([29, 27]\)).

### References


